

## Learning outcomes and competences

At the end of the course unit the learner is expected to be able to:

1. Read, write and use the language of mathematics fluently to describe problems
2. Apply the discrete mathematics concepts to the development of algorithms and programming;
3. Use the vector calculus to represent and manipulate geometric fiigures in the plane and in the space;
4. Use matrix calculations and transformations to work with vectors and geometric figures in the plane and in the space.

## Prerequisites

Before the course unit the learner is expected to be able to
Understand the use of Mathematics - medium level

## Course contents

Topics of Discrete Mathematics: propositional calculus; set theory; sequences and proportions. Topics of Geometry: matrix calculation; trigonometry; vector calculus in plane and space; geometric transformations.

## Course contents (extended version)

1. Topics in Discrete Mathematics

- Logical operations on proposals: negation, conjunction, disjunction, implication and equivalence;
-Truth tables and properties of the propositional calculus
- Logical operations on conditions and expressions with variables and quantifiers
- Equality of sets: extension axiom and set cardinality; inclusion;
- Union, intersection, complementary sets, cartesian product and powerset of a sets;
- Properties of set operation and Venn's diagrams;
- Defining sequences by general formula and recursively;

Fibonacci sequence
Proportions and golden ratio
2. Topics in Geometry

- Matrices. Definitions. Operations with matrices and properties.

The inverse matrix. Transpose of a matrix.
Determinant of a matrix of 1 st, 2nd and 3rd order.
Trigonometry. Pythagorean trigonometry identity and formulas
Trigonometric relations; remarkable values. Solving triangles.
Vectorial calculus. Representing points and vectores in aorthonormal reference; a standard vector.

- Vector operations: adiction, scalar product, normalization and polar form.
- Lines and planes, circles and spheres. Related position. Dot product and cross product.
- Polygon and polyhedra. Some properties.
- Geometric transformations. Rotation, translation, reflection, scale and projection.


## Recommended reading

1. Epp, S. (2011). Discrete Mathematics and Applications, 4th edition, Brooks/Cole CENGAGE Learning [ISBN-10: 0-495-82616-2 | ISBN-13: 978-0-495-82616-3]
2. Corbalán, F. (2016) A PROPORÇĀO ÂUREA A linguagem matemática da beleza. National Geographic, Portugal
3. Kalajdzieyski, S. (2008) MATH and ART an introduction to visual mathematics. CRC Press [ISBN: 978-1-58488-913-7]
4. Anton, H. \& Rorres, C. (2010). Elementary Linear Algebra with Applications. (10th ed. ) Wiley. [ISBN: 0470432055]

## Teaching and learning methods

Presentation of theoretical aspects of subjects in lectures using simple examples. Realization, on the part of the students, of practical exercises of application of the theoretical concepts in practical sessions tutorials. Individual work to be done outside of class and group work inside and outside the class, promoting the debate of ideas and joint resolution of proposed problems.

## Assessment methods

- Final Evaluation (incoming students) - (Regular, Student Worker) (Final, Supplementary, Special)
- Practical Work - 50\% (3 out of 4 possible)
- Final Written Exam - 50\% (All syllabus (minimum mark 7 points in 20))


## Language of instruction

Portuguese, with additional English support for foreign students.
Electronic validation

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