

Course Unit	Discrete Mathematics	Field of study	Mathematical and Quantitative Methods
Bachelor in	Informatics and Communications	School	School of Public Management, Communication and Tourism
Academic Year	2023/2024	Year of study	1
Type	Semestral	Semester	1
Workload (hours)	162	Contact hours	T - , TP 60, PL - , TC - , S - , E - , OT 20, O -
Level	1-1	ECTS credits	6.0
Code	9188-320-1103-00-23		

T - Lectures; TP - Lectures and problem-solving; PL - Problem-solving, project or laboratory; TC - Fieldwork; S - Seminar; E - Placement; OT - Tutorial; O - Other

Name(s) of lecturer(s) Ines Monteiro Barbedo de Magalhaes

### Learning outcomes and competences

At the end of the course unit the learner is expected to be able to:

1. get the logical value of a logical expression known its entrances; simplify logical expressions;
2. know the operations on sets and apply them in problem solving;
3. know some counting techniques and apply them in problem solving;
4. read numbers in some bases and to convert them to different bases; capable to operate in fixed and floating point;
5. prove conjectures using the method of mathematical induction;
6. operate in modular arithmetic; identify order relations;
7. construct graphs and identify its proprieties;
8. determine spanning trees and optimal paths in connected graphs.

### Prerequisites

Before the course unit the learner is expected to be able to:  
use the language and elementary techniques of mathematics learned in secondary and basic education.

### Course contents

Propositional Calculus. Elementary set theory. Elementary counting techniques. Numeral systems. Induction and recursion. Binary relations. Introduction on graph theory.

### Course contents (extended version)

1. LOGIC
  - Propositional Calculus;
  - Logical operations on proposals: negation, conjunction and disjunction;
  - Implication and equivalence;
  - Truth tables;
  - Properties of the propositional calculus;
  - Logical operations on conditions;
  - Expressions with variables;
  - Quantifiers;
  - Simplification of logical expressions.
2. ELEMENTARY SET THEORY
  - Equality of sets: extension axiom;
  - Inclusion;
  - Null set and singular set;
  - Union, intersection and complementary sets;
  - Venn's diagrams;
  - Cartesian product and powerset of a sets;
  - Properties of set operation;
  - Cardinality.
3. ELEMENTARY COUNTING TECHNIQUES
  - The addition rule, inclusion- exclusion rule and multiplication rule;
  - Simple arrangements and composites, permutations;
  - Combinations;
  - Arrangement and combination with repetition.
4. NUMERAL SYSTEMS
  - Positional and non-positional numeral systems;
  - Numeral bases and decimal, binary, octal and hexadecimal bases;
  - Converting from decimal base to other bases;
  - Converting between binary, octal and hexadecimal bases;
  - Signed integers representations: sign-magnitude and complements;
  - Fixed-point arithmetic;
  - Floating-point representation.
5. INDUCTION AND RECURSION
  - Sequences. Defining sequences by general formula and recursively;
  - Mathematical induction;
  - Proving properties by induction.
6. BINARY RELATIONS
  - Definition and properties of the binary relations;
  - Equivalence relation and class of equivalence;
  - Congruencies: examples of application;
  - Order relations and Hasse diagrams.
7. INTRODUCTION TO GRAPH THEORY
  - Simple graphs, connected, bipartite, complete graphs, Euler graphs and Hamilton;
  - Minimum spanning tree - Kruskal's algorithm and Prim's algorithm;
  - Digraphs;
  - Binary tree of Huffman's algorithm.

### Recommended reading

1. CARDOSO, D. , SZYMANSKI, J. & ROSTAMI, M. (2009). Matemática Discreta: Combinatória, Teoria dos Grafos, Algoritmos. Escolar Editora [ISBN-13: 978-972-592-237-8]
2. EPP, Susanna (2011). Discrete Mathematics and Applications (4th ed. ). Brooks/Cole CENGAGE Learning [ISBN-13: 978-0-495-82616-3]
3. GOODAIRE, E. G. & PARMENTER, M. (2006). Discrete Mathematics with Graph Theory. (3rd ed. ). Pearson [ISBN-13: 978-0131679955]

**Recommended reading**

4. LEVIN, Oscar (2018). Discrete Mathematics An open introduction (3rd ed. ). SMS University of Northern Colorado [ISBN-13: 978-1792901690]
5. BARBEDO, Inês (2018) Apontamentos de Matemática Discreta, EsACT

**Teaching and learning methods**

For each subject they are considered periodically, with antecedence, modules of work with communication of the contents; solved exercises; exercises of guided resolution; complementary exercises, stimulating the work in equips; The lessons will be guided in the direction of to check the difficulties of execution of the considered works; to explain contents and examples on the practical cases.

**Assessment methods**

- Final Evaluation (incoming students) - (Regular, Student Worker) (Final, Supplementary, Special)
- Practical Work - 50% (3 out of 4 possible)
- Final Written Exam - 50% (All syllabus (minimum mark 7 points in 20))

**Language of instruction**

Portuguese, with additional English support for foreign students.

**Electronic validation**

Ines Monteiro Barbedo de Magalhaes	Vítor José Domingues Mendonça	Anabela Neves Alves de Pinho	Luisa Margarida Barata Lopes
13-10-2023	13-10-2023	15-10-2023	16-10-2023